$\qquad$
$\qquad$

# GUJARAT TECHNOLOGICAL UNIVERSITY <br> BE- SEMESTER $1^{\text {st }} / 2^{\text {nd }}$ EXAMINATION (NEW SYLLABUS) - SUMMER - 2017 

## Subject Code: 2110014

Date:01/06/2017
Subject Name: Calculus
Time: 2:30 PM to 05:30 PM
Total Marks: 70

## Instructions:

1. Question No. 1 is compulsory. Attempt any four out of remaining Six questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

## Q. $1 \quad$ Objective Question (MCQ)

(a) Choose the appropriate answer for the following question.

1. Infinite series
 $\qquad$ .
(A) Divergent
(B) Convergent
(C) Oscillation
(D) None of these
 $\qquad$ .
(A) 禺
(B) $\log (1+x)$
(C) $\sin x$
(D) $\cos x$
2. The value of the lino
(A) 2
(B) 1
(C) -1
(D)
3. Asymptote parallel to $y$-axis of the curve $y=$ in e the line $\qquad$ .
(A) $x=0$
(B) $\mathrm{y}=0$
(C) $x=2$
(D) $y=2$
4. $f(x)=\rrbracket$ 涊 $\|$ is $\qquad$ at origin.
(A) continuous
(B) discontinuous
(C) differentiable
(D) None of these
5. Curve $y^{2}(a+x)=x^{2}(b-x)$ is symmetric about $\qquad$ _.
(A) x - axis
(B) $y$ - axis
(C) line $\mathrm{x}=\mathrm{b}$
(D) line $x=-a$
6. The curve increases strictly in the interval in which $\qquad$ -
(A) $<0$
(B) $>0$
(C) $=0$
(D) None of these
(b) Choose the appropriate answer for the following question.
7. The values of fur waves $\qquad$ .
(A) 0
(B) -
(C)
(D)
8. What does the region $f_{i}^{x}$ delsodhy $=$ $\qquad$ .
(A) rectangle
(B) square
(C) circle
(D) triangle
9. The values of the

(A) 0
(B) 1
(C) -1
(D)
10. The function $f(x, y)=x^{2} y f(y / x)$ is homogeneous of degree is $\qquad$ .
(A) 0
(B) 1
(C) 2
(D) 3
11. The equation of the form $f(x y)=c$, then ${ }_{x}$ $\qquad$ .
(A)
(B)
(C) -
(D)
12. The values of

$\qquad$ -
(A) 0
(B) 1
(C) -1
(D)

is $\qquad$ -.
(A) 4
(B) -1
(C) 5
(D) 7
Q. 2 (a) Expand $\log (\sec x)$ in power of $x$.
(b) Evaluate
(c) (i) Trace the curve $y^{2}(2 a-x)=x^{3}$.
(ii) determine
Q. 3 (a) If $f(x, y)=x^{2} y+x y^{2}$ then find $f_{x}(1,2)$ and $f_{y}(1,2)$ by definition.
(b) Check the continuity for the following function at $(0,0)$


$$
=0, \quad(x, y)=(0,0)
$$

(c)
(i) if $u=4.0$


Q. 4 (a) Find the extreme values of $x^{3}+3 x y^{2}-3 x^{2}-3 y^{2}+4$.
(b) Find the equation of the tangent plane and normal line to the surface $2 x^{2}+$ 03 $\mathrm{y}^{2}+2 \mathrm{z}=3$ at $(2,1,-3)$
(c) (i) Find a point on the plane $2 x+3 y-z=5$ which is nearest to the origin.
(ii) Expaned $\sqrt{4}$ in power of $\mathrm{x}-1$ and $\mathrm{y}-1$ using Taylor's expansion.
Q. 5 (a) Test for the convergence the series;
(b) Test for the convergence the series;

(c) (i) Determine absolute or conditional convergence of the series;



(b) Sketch the region of integration and evaluate
(c) (i) Evaluate the integral
 by changing the order of integration.
(ii) Evaluate the integral $n^{2}$.
Q. 7 (a) Find the area included between the curve $y^{2}(2 a-x)=x^{3}$ and its asymptote.
(b) Find the volume of a solid generated by revolving the cardioid $r=a\left(1+\cos { }^{2}\right)$ about the initial line.
(c) Use triple integration to find the volume of the solid within the cylinder $\mathrm{x}^{2}+\mathrm{y}^{2}=9$ between the planes $\mathrm{z}=1$ and $\mathrm{x}+\mathrm{z}=1$.

