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## GUJARAT TECHNOLOGICAL UNIVERSITY MCA- SEMESTER- II• EXAMINATION - WINTER 2017

## Subject Code: 2620004

Subject Name: Computer Oriented Numerical Methods
Time:02:30pm TO 05:00pm

## Instructions:

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
Q. 1 (a) What is Total Numerical Error? Explain different types of numerical errors with suitable example.
(b) Use Gauss-Seidel method to find the solution of the following system of equations.

$$
\begin{aligned}
& 20 x+2 y+z=30 \\
& x-40 y+3 z=-75 \\
& 2 x-y+10 z=30
\end{aligned}
$$

Q. 2 (a) Use bisection method to find the root of the equation $x^{3}-9 x+1=0$, in the interval[0,1], correct up to two significant digit accuracy.
(b) Use false-position method to find a root of the equation $x^{2}-17$ correct up to three significant digit accuracy.

OR
(b) the polynomial equation $f(x)=2 x^{3}-5 x+1=0$,taking initial value as using Birge-Vieta Method up to two significant digit accuracy.
Q. 3 (a) Find the interpolation polynomial which takes following values by using Newton's Forward Difference Interpolation.(hint $\mathrm{x}_{0}=0, \mathrm{~h}=1$ )

| X | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 41 | 43 | 47 | 53 | 61 | 71 |

(b) Fit a straight line $\mathrm{y}=\mathrm{ax}+\mathrm{b}$ to the following data by the method of least square.

| X | 3.4 | 4.3 | 5.4 | 6.7 | 8.7 | 10.6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 4.5 | 5.8 | 6.8 | 8.1 | 10.5 | 12.7 | OR

Q. 3 (a) Derive an expression for Newton's Backward Difference interpolation formula with example.
(b) Using Lagrange's Interpolation, find the value of $f(0)$ at the table given below

| X | -1 | -2 | 2 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(\mathrm{X})$ | -1 | -9 | 11 | 69 |

Q. 4 (a) Evaluate $f(9)$ by using Newton's Divided Difference Interpolation Formula.

| X | 5 | 7 | 11 | 13 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 150 | 392 | 1452 | 2366 | 5202 |

(b) Find a root of equation $x^{3}-2 x-5=0$ using Secant Method correct to three significant digit accuracy.
Q. 4 (a) Use Gauss-Elimination method to find the solution of the following system of equations, find $\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3}$.

$$
\begin{gathered}
\mathrm{x}_{1}+2 \mathrm{x}_{2}+\mathrm{x}_{3}=0 \\
2 \mathrm{x}_{1}+2 \mathrm{x}_{2}+3 \mathrm{x}_{3}=3 \\
-\mathrm{x}_{1}-3 \mathrm{x}_{2}=2
\end{gathered}
$$

(b) Find out $\mathrm{A}+\mathrm{B}, \mathrm{A}-\mathrm{B}, 3 \mathrm{~A}+4 \mathrm{~B}$ and $3 \mathrm{~A}-4 \mathrm{~B}$ form given data,

$$
\mathrm{A}=\left[\begin{array}{rrr}
1 & 3 & -2 \\
4 & 6 & 7 \\
2 & -5 & 0
\end{array}\right] \quad \mathrm{B}=\left[\begin{array}{ccc}
10 & 5 & -4 \\
0 & -7 & -8 \\
9 & 11 & 6
\end{array}\right]
$$

Q. 5 (a) The following table shows age( X ) and blood pressure $(\mathrm{Y})$ of 8 persons, obtain the Regression equation of Y on X and also find the expected blood-pressure of a person who is 49 years old.

| X | 52 | 63 | 45 | 36 | 72 | 65 | 47 | 25 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 62 | 53 | 51 | 25 | 79 | 43 | 60 | 33 |

(b) From the following data fit a straight line and parabola, also find which fit is

More reliable.

| X | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 1 | 5 | 10 | 22 | 38 |

## OR

Q. 5 (a) Apply Runge-Kutta $4^{\text {th }}$ order method to find $y(0.1)$,if $d y / d x=x^{2}+2 y$ $y(0)=-1, h=0.1$
(b) Define any six type of matrix with example.

